

AM-305 M3

pet 11³⁰ - 12³⁰ → g. ure

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lab vaje od 24.10. →

seminar: 3 ned. stare starke

- zbirka nalog - Dig strukture G. Pucihar, T. Kotnik
- rešeni primeri iz prelopljenih vezij - A. Stepanovski
- prelopljena vezja in strukture, priročnik za vaje - M. Trebar

$$x \in \{0, 1\}$$

$$1+1 \neq 2$$

= 1 → logično seštevanje - AND funkcija

1. BOOLE-OVA ALGEBRA

$$x \in \{0, 1\}$$

- disjunkcija → "OR" → "+" → $x + y$
 - konjunkcija → "AND" → "·" → $x \cdot y$
 - negacija → "NOT" → "-" → $\bar{x}$
- } s temi funkcijami opisemo vse.

$$0 \quad 1 \quad 0 \quad 1$$

0, 1 predstavljata napetostne nivoje

1.1 Osnovna pravila:

$$\begin{aligned} 1+1 &= 1 \cdot 1 = 1 \\ 0+0 &= 0 \cdot 0 = 0 \\ 0+1 &= 1+0 = 1 \\ 0 \cdot 1 &= 1 \cdot 0 = 0 \end{aligned}$$

1.2 Postulati:

P1) $x+0 = x$	P1') $x \cdot 1 = x$
P2) $x+y = y+x$	P2') $x \cdot y = y \cdot x$
P3) $x+(y \cdot z) = (x+y) \cdot (x+z)$	P3') $x(y+z) = x \cdot y + x \cdot z$
P4) $x+\bar{x} = 1$	P4') $x \cdot \bar{x} = 0$

1.3 Teoremi:

$$\begin{aligned} x+1 &= 1 \\ x \cdot x &= x \end{aligned}$$

dokaz: $x \cdot x \stackrel{P1}{=} x \cdot x + 0 \stackrel{P4'}{=} x \cdot x + x \cdot \bar{x} \stackrel{P3'}{=} x(x + \bar{x}) =$
 $\stackrel{P4}{=} x \cdot 1 \stackrel{P1'}{=} x$

$$X + X \cdot Y = X$$

$$\rightarrow \text{doka} \dot{z}: X + X \cdot Y \stackrel{P1}{=} X \cdot 1 + X \cdot Y \stackrel{P3}{=} X \cdot (1 + Y) \stackrel{T1=1}{=} X \cdot 1 = \underline{X}$$

1.4 DeMorgan:

$$\overline{X+Y} = \overline{X} \cdot \overline{Y} \rightarrow \text{doka} \dot{z} \text{ (s pravilnostno tabelo)}$$

$$\overline{X \cdot Y} = \overline{X} + \overline{Y}$$

X	Y	X+Y	$\overline{X+Y}$	$\overline{X} \cdot \overline{Y}$	$\overline{X \cdot Y}$
0	0	0	1	1	1
0	1	1	0	0	0
1	0	1	0	0	0
1	1	1	0	0	0

S pravili B, algebre poenostavimo naslednji izraz:

$$a) f = A \cdot B + B \cdot (B + \overline{C}) + \overline{B} \cdot C$$

$$f = AB + BB + B\overline{C} + \overline{B}C =$$

$$B \cdot B = B$$

$$= AB + B + B\overline{C} + \overline{B}C =$$

$$= B(A + 1 + \overline{C}) + \overline{B}C =$$

$$= B \cdot 1 + \overline{B}C \quad \text{kao "X" + 1 = 1}$$

$$= B + \overline{B}C \stackrel{P3}{=}$$

$$= \underbrace{(B + \overline{B})}_{1} \cdot (B + C) = \underline{B + C}$$

$$b) f = A\overline{B} + \overline{C}(\overline{A} + B)$$

$$f = A\overline{B} + \overline{C}(\overline{A} \cdot \overline{B}) =$$

$$= A\overline{B} + \overline{C}(A\overline{B}) =$$

$$= A\overline{B} + A\overline{B}\overline{C} =$$

$$= A\overline{B} \underbrace{(1 + \overline{C})}_1 = \underline{A\overline{B}}$$

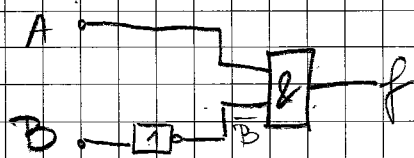
← "izpitna naloga"

1.5 logična vrata:

AND $\boxed{\&}$

OR $\boxed{\geq}$

NOT $\boxed{1}$



$$A = 1$$

$$B = 0$$

$$f = ?$$

$$f = 1 \cdot 0 = 1 \cdot 1 = \underline{1}$$

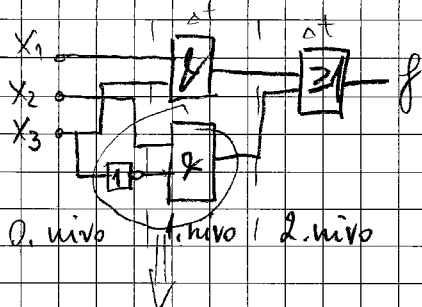
Poiščite minimalno obliko funkcije in narišite vezje:

20.10.2011

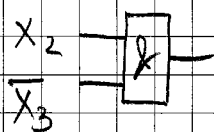
$$f(x_1, x_2, x_3) = x_1 \bar{x}_2 x_3 + x_2 (\bar{x}_3 + x_1 \cdot x_3) =$$

$$= x_1 \bar{x}_2 x_3 + x_2 \bar{x}_3 + x_1 x_2 x_3 = x_1 x_3 (\underbrace{\bar{x}_2 + x_2}_1) + x_2 \bar{x}_3 =$$

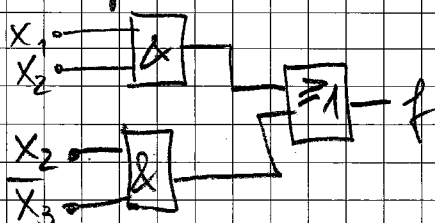
$$= x_1 x_3 + x_2 \bar{x}_3$$



2-nivojska realizacija → normalna



funkcijo na izhodu vezja napišite v obliki pravilnostne tabele:



$$f = x_1 x_2 + x_2 \bar{x}_3$$

x_1	x_2	x_3	f
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

Poiščite analitični zapis funkcije podane s tabelo in narišite vezje.

x_1	x_2	x_3	f
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

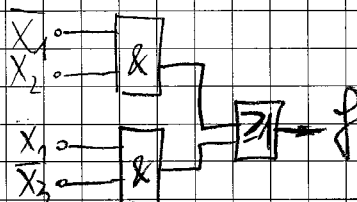
a) "1" $f = \bar{x}_1 \bar{x}_2 \bar{x}_3 + x_1 \bar{x}_2 x_3 + x_1 \bar{x}_2 x_3 + x_1 x_2 \bar{x}_3$ ← disjunktivna oblika funkcije s produktov je popolna PDNO

$$f = \bar{x}_1 \bar{x}_2 (\bar{x}_3 + x_3) + x_1 \bar{x}_2 (\bar{x}_2 + x_2) = \bar{x}_1 \bar{x}_2 + x_1 \bar{x}_2$$

$$f = \bar{x}_1 \bar{x}_2 + x_1 \bar{x}_3$$

← minimalna oblika disjunktivna MDNO

(najbolj skrajšana funkcija)



2-nivojska / normalna oblika
AND-OR oblika

b) "0"

$$\bar{f} = \bar{x}_1 \bar{x}_2 \bar{x}_3 + \bar{x}_1 \bar{x}_2 x_3 + x_1 \bar{x}_2 x_3 + x_1 x_2 x_3$$

$$\bar{f} = \bar{x}_1 \bar{x}_2 (\bar{x}_3 + x_3) + x_1 \bar{x}_2 x_3 + x_1 x_2 x_3 = \bar{x}_1 \bar{x}_2 + x_1 \bar{x}_2 x_3 + x_1 x_2 x_3$$

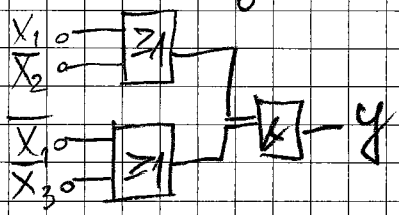
$$= (\bar{x}_1 + x_1) \cdot (\bar{x}_2 + x_2) \cdot (\bar{x}_3 + x_3) = 1 \cdot 1 \cdot 1 = 1$$

popolna konjunktivna oblika

PKO 4

P3: $X + (Y \cdot Z) = (X + Y) \cdot (X + Z)$

$f = (X_1 + \overline{X_2} + \underbrace{X_3 \cdot \overline{X_3}}_0) \cdot (\overline{X_1} + \overline{X_3} + \underbrace{X_2 \cdot \overline{X_2}}_0) = (X_1 + \overline{X_2}) \cdot (\overline{X_1} + \overline{X_3})$ minimalna konjunktivna oblika
MKNO



$\overline{X_1}X_2 + X_1\overline{X_3} = (X_1 + \overline{X_2}) \cdot (\overline{X_1} + \overline{X_3})$?

f MKNO
 $= \underbrace{X_1\overline{X_1}}_0 + X_1\overline{X_3} + \overline{X_2}\overline{X_1} + \overline{X_2} \cdot \overline{X_3} =$
 $= \underbrace{X_1\overline{X_3} + \overline{X_2}\overline{X_1}}_{\overline{X_1}\overline{X_3} + \overline{X_2}\overline{X_1}} + \overline{X_2} \cdot \overline{X_3} \cdot (X_1 + \overline{X_1}) =$
 $= X_1\overline{X_3} + \overline{X_2}\overline{X_1} + X_2\overline{X_3} \cdot X_1 + \overline{X_2}\overline{X_3} \cdot \overline{X_1}$
 $X_1\overline{X_3} (1 + \overline{X_2}) + \overline{X_2}\overline{X_1} (1 + X_3) = \underline{X_1\overline{X_3} + \overline{X_2}\overline{X_1}} = \underline{f_{MKNO}}$

KARNAUGH - jevi DIAGRAMI

Poenostavimo funkcijo izprejšnji naloge s K diagramom:

		$X_1 \backslash X_2$			
		00	01	11	10
X_3	0	1	0	1	1
	1	1	0	0	0

$f: \overline{X_1}\overline{X_2} + X_1\overline{X_3}$

Zapišimo M_2 v K-diagram:

$M_2 = (\overline{X_1} + X_2 + \overline{X_3})$

		00	01	11	10
0					
1					

$M_2 = m_5$

$X_1\overline{X_2}X_3 = m_5$

27.10.2011

$f(X_1, X_2, X_3) = M_1 \cdot M_3 \cdot M_7 = \prod 1, 3, 7 = (\overline{X_1} + \overline{X_2} + \overline{X_3}) \cdot (\overline{X_1} + X_2 + X_3) \cdot (X_1 + X_2 + X_3)$

$= m_7 + m_5 + m_3 + m_2 + m_1 = \Sigma 1, 2, 3, 5, 7 =$

$= X_1X_2X_3 + \overline{X_1}X_2X_3 + X_1\overline{X_2}X_3 + \overline{X_1}\overline{X_2}X_3 + X_1X_2\overline{X_3}$

PDNO

PKNO

7	6	5	4	3	2	1	0	M
0	1	2	3	4	5	6	7	M

		$X_1 \backslash X_2$			
		00	01	11	10
X_3	0		1		
	1	1	1	1	1

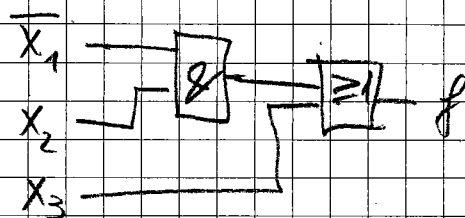
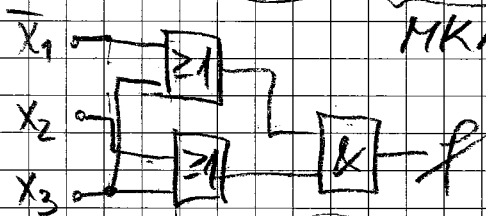
$$= X_3 + \bar{X}_1 X_2$$

MDNO

$X_1 \backslash X_2$	00	01	11	10
0	0	0	0	0
1	0	0	0	0

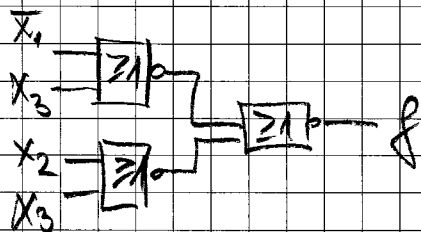
$$= (\bar{X}_1 + X_3) \cdot (X_2 + X_3)$$

MKNO

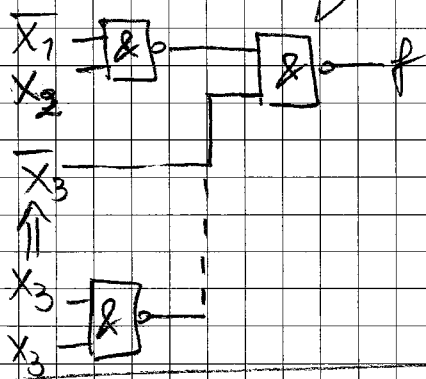


$$\overline{X_3 + \bar{X}_1 X_2} = \overline{X_3 \cdot \bar{X}_1 X_2} = \overline{X_3 X_3 \cdot \bar{X}_1 X_2} = \overline{(\bar{X}_1 + X_3) \cdot (X_2 + X_3)} = \downarrow(\downarrow(\bar{X}_1 + X_3), \downarrow(X_2 + X_3))$$

NOR

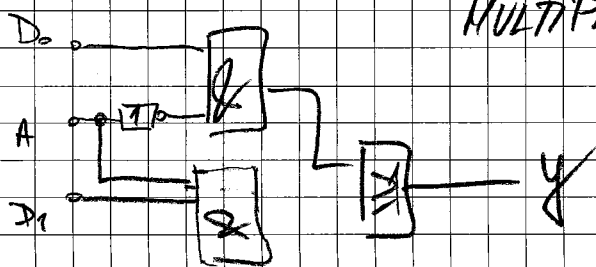


potrebujemo samo 1 čip, ki ima 4 dvostrukih NOR vrat
tudi negacijo lahko izvedemo z NOR



MULTIPLESOR - MUX

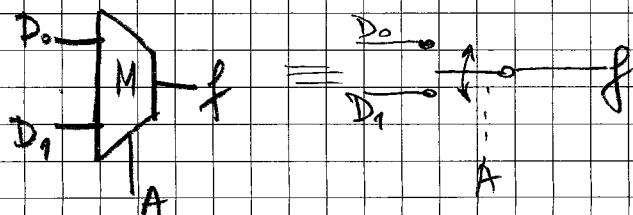
3. 11. 2011



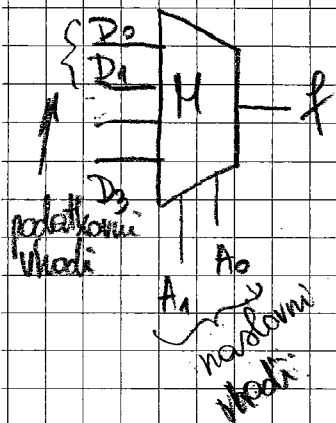
$$f = \bar{A} D_0 + A D_1$$

$$A=0 \Rightarrow f=D_0$$

$$A=1 \Rightarrow f=D_1$$



STIKALO



$$f = m_0 D_0 + m_1 D_1 + \dots + m_{2^n-1} D_{2^n-1}$$

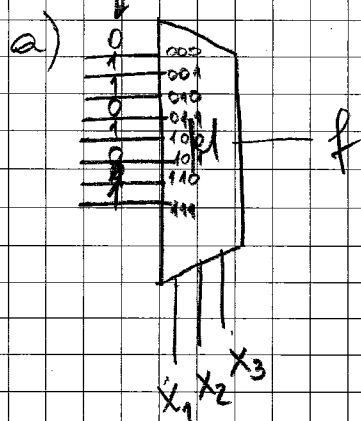
$\downarrow$ $\downarrow$
 $A_1 A_0$ $A_1 A_0$

samo podatkovni vhodi gredo na izhod

Preklopno funkcijo realizirajte z MUX z 8, 4, 2 ^{podatkovnimi} vhodi.

$$f(x_1, x_2, x_3) = \sum_{a) b) c)} 1, 2, 4, 6, 7$$

$$f = \overline{x_1} \overline{x_2} x_3 + \overline{x_1} x_2 \overline{x_3} + x_1 \overline{x_2} \overline{x_3} + x_1 x_2 \overline{x_3} + x_1 x_2 x_3$$

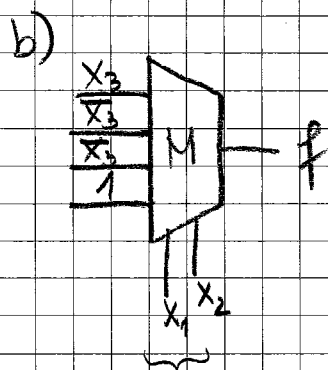


x_1	x_2	x_3	Σ
0	0	0	0
0	0	1	1
0	1	1	1
1	0	1	1
1	1	0	0
0	0	1	1
1	0	1	1
1	0	1	1
1	1	1	1

$$\overline{x_1} \overline{x_2} x_3 (0) + \overline{x_1} x_2 \overline{x_3} (1) + x_1 \overline{x_2} \overline{x_3} (1) + \dots + x_1 x_2 x_3 (1)$$

MUX
8-1 ali 8/3

0 → masa
1 → Vcc



$$f = \underbrace{\overline{x_1} \overline{x_2}}_{m_0} (\underbrace{x_3}_{D_0}) + \underbrace{\overline{x_1} x_2}_{m_1} (\underbrace{\overline{x_3}}_{D_1}) + \underbrace{x_1 \overline{x_2}}_{m_2} (\underbrace{x_3}_{D_2}) + \underbrace{x_1 x_2}_{m_3} (\underbrace{\overline{x_3} + x_3}_1)$$

MUX
4/1 ali 4/2

izberemo si dve od treh spremenljivk (po navadi izberemo tiste, ki se pojavita v vseh členih)

$$c) f = \bar{X}_1 \bar{X}_2 X_3 + \bar{X}_1 X_2 \bar{X}_3 + X_1 \bar{X}_2 \bar{X}_3 + X_1 X_2 \bar{X}_3 + X_1 X_2 X_3$$

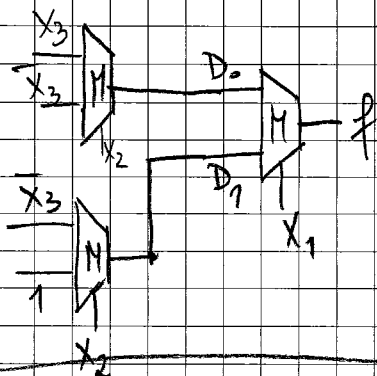
MUX 2-1 ali 2/1

ker so nam ostale funkcije dodamo še 2 MUX-a v kaskado

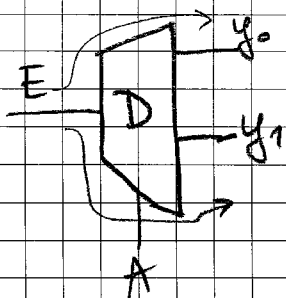
$$\bar{X}_1 (\underbrace{\bar{X}_2 X_3 + X_2 \bar{X}_3}_{D_0}) + X_1 (\underbrace{\bar{X}_2 \bar{X}_3 + X_2 \bar{X}_3 + X_2 X_3}_{D_1})$$

$$D_0 = \bar{X}_2 X_3 + X_2 \bar{X}_3 = \bar{X}_2 (X_3) + X_2 (\bar{X}_3)$$

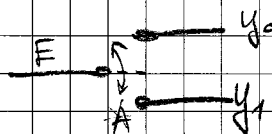
$$D_1 = \bar{X}_2 \bar{X}_3 + X_2 \bar{X}_3 + X_2 X_3 = \bar{X}_2 (\bar{X}_3) + X_2 (\underbrace{\bar{X}_3 + X_3}_1)$$



DEMULTIPLEKSOR - DEMUX



$\equiv$



$$A=0 \Rightarrow y_0 = E$$

$$A=1 \Rightarrow y_1 = E$$

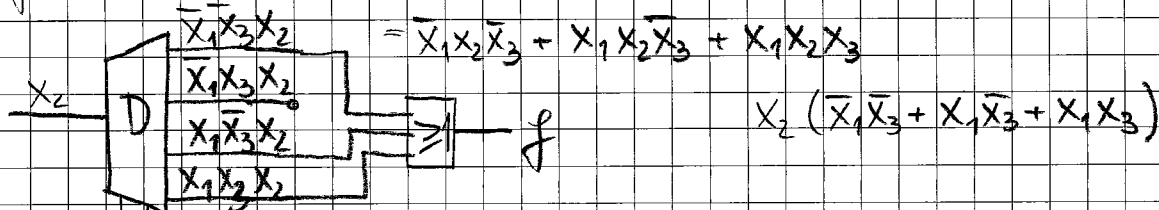
$$y_0 = m_0 \cdot E$$

$$y_1 = m_1 \cdot E$$

$$y_{2^n-1} = m_{2^n-1} \cdot E$$

Preklopno f. realizirajte z DEMUX s štirimi izhodi in OR vrati

$$f(X_1, X_2, X_3) = \sum 2, 6, 7 =$$



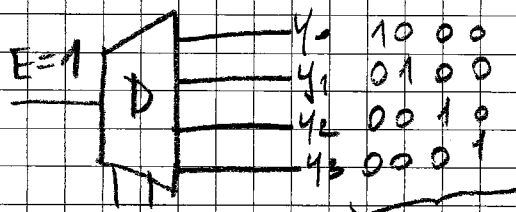
$$= \bar{X}_1 \bar{X}_2 \bar{X}_3 + X_1 X_2 \bar{X}_3 + X_1 X_2 X_3$$

$$X_2 (\bar{X}_1 \bar{X}_3 + X_1 \bar{X}_3 + X_1 X_3)$$

DEMUX
2/4
1-4

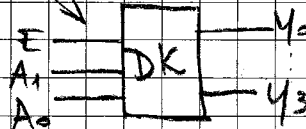
$(X_1 \bar{X}_3)$

KAJ DOBIMO NA IZHODU, CE JE NA VNHODU VEDNO 1?



A₁ A₀
0 0
0 1
1 0
1 1

DEKODIRNIK



10.11.2011

Zapiši funkcijo v MKNO:

$$f = \bar{X}_1 \bar{X}_3 X_4 + \bar{X}_2 X_3 X_4 + X_1 \bar{X}_3 X_4 + X_2 X_3 X_4$$

	X ₁ X ₂			
	00	01	11	10
X ₃ X ₄	00	0	0	0
	01	1	1	1
	11	1	1	1
	10	0	0	0

$$f_{MNO} = X_4$$

$$f_{MKNO} = X_4$$

2 različna zapisa iste funkcije

$$f = (\bar{X}_2 + \bar{X}_3) \cdot (\bar{X}_1 + X_2 + X_3) \cdot (\bar{X}_1 + X_2 + X_4)$$

	X ₁ X ₂			
	00	01	11	10
X ₃ X ₄	00	1	1	0
	01	1	1	0
	11	1	0	1
	10	1	0	0

$$f_{MKNO} = X_2 X_3 + X_1 X_2 + X_1 X_4$$

$$f_{MKNO} = (\bar{X}_2 + \bar{X}_3) \cdot (\bar{X}_1 + X_2) \cdot (\bar{X}_1 + X_4)$$

$$f_{MNO} = \bar{X}_1 \bar{X}_2 + \bar{X}_1 \bar{X}_3 + \bar{X}_2 X_4$$

Veje - pri katerem bo na izhodu 1, če sta dvobitni številki večji od 3

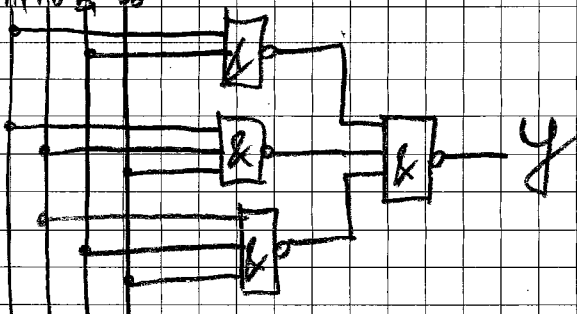
A ₁	A ₀	B ₁	B ₀
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

NAND

	A ₁ A ₀			
	00	01	11	10
B ₁ B ₀	00	0	0	0
	01	1	1	1
	11	1	1	1
	10	1	1	1

$$f_{MNO} = A_1 B_1 + A_1 A_0 B_0 + A_0 B_1 B_0$$

$$f = A_1 B_1 \cdot A_1 A_0 B_0 \cdot A_0 B_1 B_0$$



Zapišite vezje s pretvorbo BCD kode v IN3 (ex. EXCESS 3)

BCD - binarno kodirano deetiško število (0-9)

	BCD				IN-3			
	A	B	C	D	W	X	Y	Z
0	0	0	0	0	0	0	1	1
1	0	0	0	1	0	1	0	0
2	0	0	1	0	0	1	0	1
3	0	0	1	1	0	1	1	0
4	0	1	0	0	0	1	1	1
5	0	1	0	1	1	0	0	0
6	0	1	1	0	1	0	0	1
7	0	1	1	1	1	0	1	0
8	1	0	0	0	1	0	1	1
9	1	0	0	1	1	1	0	0
10	1	0	1	0				
11	1	0	1	1				
12	1	1	0	0				
13	1	1	0	1				
14	1	1	1	0				
15	1	1	1	1				

Začnemo s 3.

	W	X	Y	Z
00				
01				
11				
10				

	X	Y	Z
00			
01			
11			
10			

$$W = A + BD + BC$$

	Y	X	Z
00			
01			
11			
10			

$$Y = \overline{C}D + CD$$

$$X = B\overline{C}D + \overline{B}D + \overline{B}C$$

	Z	X	Y
00			
01			
11			
10			

$$Z = \overline{D}$$

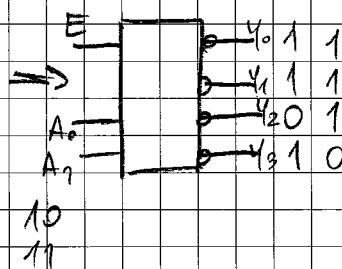
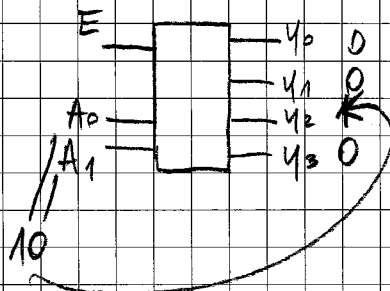
	X	Y	Z
00			
01			
11			
10			

$$f: X_2X_4 + \overline{X_2}\overline{X_4}$$

PRIPRAVA NA LAB. VA70

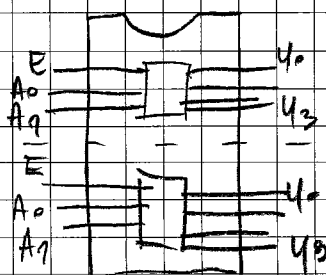
b) DEKODIRNIK

2-4

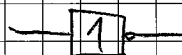


c)

3-8



$$A_2A_1A_0 - Y_0 \dots Y_7$$





entity / vmesnik (a, b, f)

architecture / zgradba

```
library IEEE;
```

```
use
```

} vključimo knjižnice

entity vrata_and is ← ime vezja

```
Port (a, b: in STD_LOGIC;
```

```
f: out STD_LOGIC);
```

end vrata_and;

```
Architecture P1 of vrata_and is
```

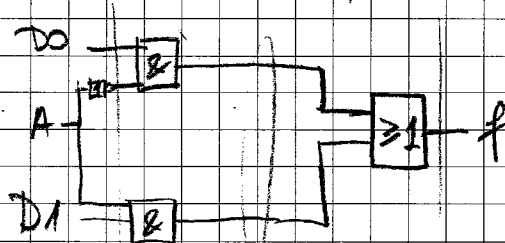
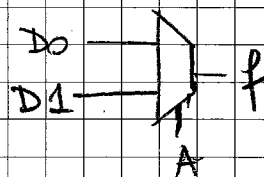
begin

```
f <- a and b;
```

end;

z when... else

z log. vrati



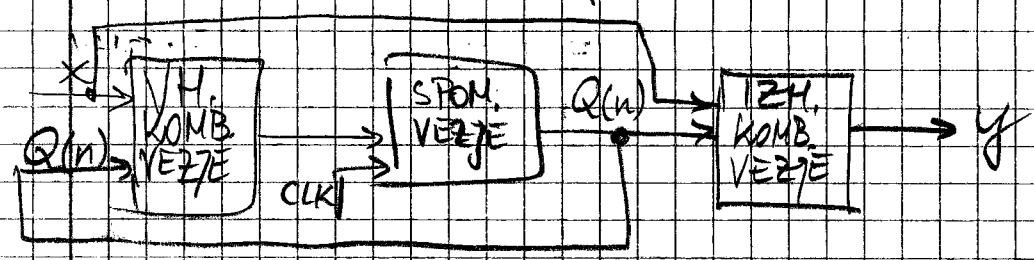
↓ 2 motranje signala

```
<= → priredimo
```

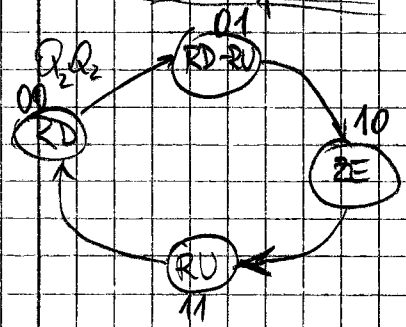
```
= → primerjamo
```

SINHRONSKA SEKVENČNA VEZJA

- komb. vezje: $y = f(x)$
- sinh...: $y(n) = f(x(n), Q(n))$; $Q(n+1) = f(x(n), Q(n))$
 izhod vhod stanje



primer: semafor



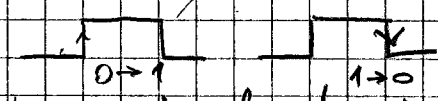
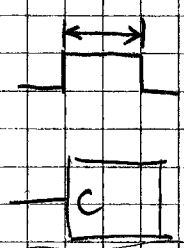
1 pomnilna celica $\begin{matrix} 0 \\ 1 \end{matrix}$

št. stanj = 2^n ; n → št. pomnilnih celic

1 celica = 2 stanja
2 celici = 4 stanja

spominke celice: zapah (latch), preklapna vezje (flip-flop)

CLK
C - control
E - enable



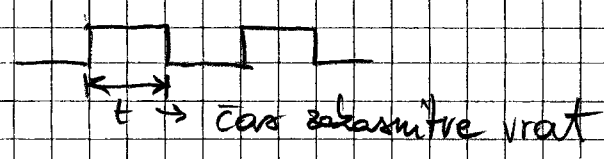
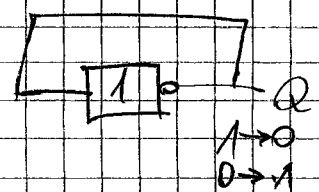
zapomne si vrednost pri prehodu
0 → 1, 1 → 0

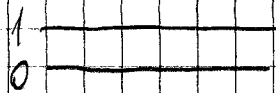
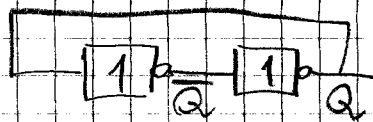
data (zapomne si kakšen je vhod in ga preneseš ne izhodi)

	S-R	T	D	JK
Latch	✓	X	✓	X
F-F	X	✓	✓	✓

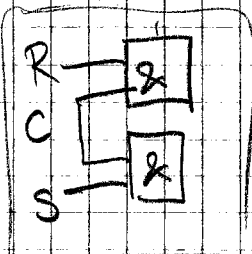
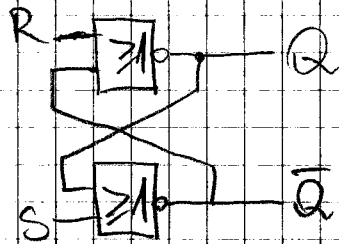
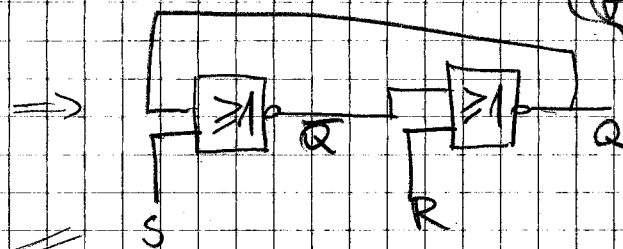
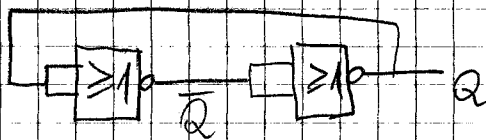
set, reset, toggle

$$y(n+1) = f(x(n), y(n))$$





negator spremeni v NOR



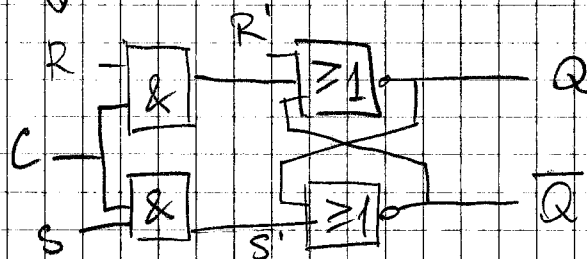
dodamo, da dobimo
sinkronizirano vrata

S=1 R=0 Q=1	S=0 R=1 Q=0	S=0 R=0 Q=Q
-------------------	-------------------	-------------------

S	R	Q	Q
0	0	Q	Q
0	1	0	1
1	0	1	0
1	1	0	0

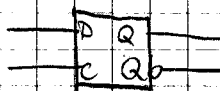
NOR		X
X ₁	X ₂	X
0	0	1
0	1	0
1	0	0
1	1	0

prevedemo stanje



RS LATCH
C=0 $\Rightarrow$ R', S' = 0 Q=Q
C=1 $\Rightarrow$ R'=R, S'=S

D - LATCH



C	D	Q	Q
0	X	Q	Q
1	0	0	1
1	1	1	0

x = 1 ali 0

D - FF



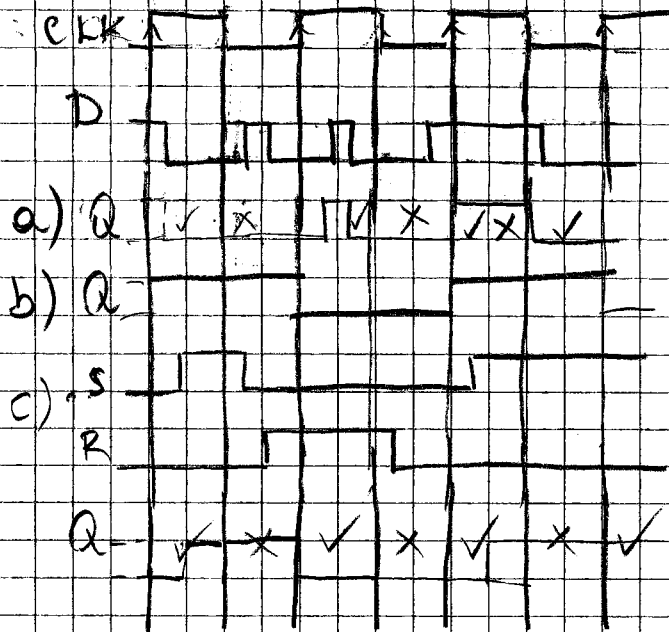
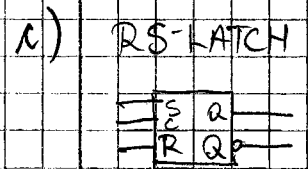
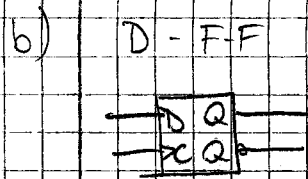
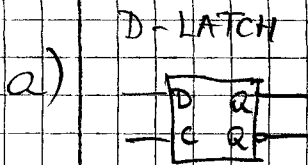
C	D	Q	Q
X	X	Q	Q
0	0	0	1
1	1	1	0

x = 1 ali 0 ali $\frac{1}{2}$

neg. fronte

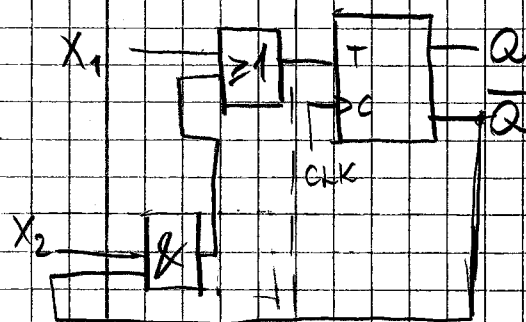
NALOGA 4.1

- zbirka rešenih nalog



1.) Analizirajte podano sek. vezje in narišite diagram stanj.

15.12.2011



S	Q
S ₀	0
S ₁	1

$$T = X_1 + X_2 \bar{Q}$$

X ₁	X ₂	Q _n	Q _{n+1}	T(n)
0	0	0	0	0
0	1	0	1	1
1	0	1	1	0
1	1	0	1	1
1	0	1	0	1
1	1	0	1	1
1	1	1	0	1

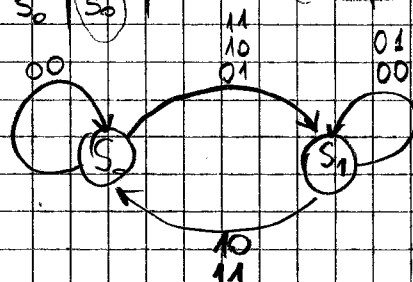
Vh. komb. vezje spom. vezje

Tabela prehodnih stanj:

X	0	0	1	1	0	1	1
Q _n	0	0	1	1	0	1	1
S ₀	S ₀	S ₀	S ₁	S ₁	S ₁	S ₀	S ₀
S ₁	S ₁	S ₁	S ₁	S ₀	S ₀	S ₁	S ₁

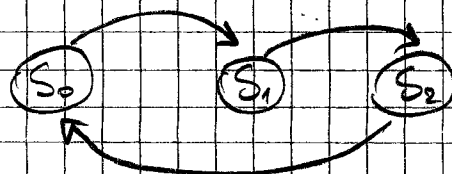
Koje T=1, se Q_{n+1} spremeni

primerjamo spremembe



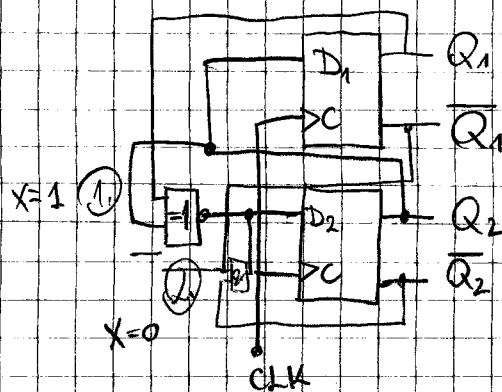
2.) Zgradite sinhronski števec, ki šteje navzgor po modulu 3 (uporabi D-flip-flop)

MODUL 3 → 3 stanj, šteje → 0, 1, 2, 0, 1, 2, 0, ...



3 stanja ⇒ 2 spom. celici
št. stanj = 2² → št. števec. celic

S	Q ₁	Q ₂
S ₀	0	0
S ₁	0	1
S ₂	1	0
S ₃	1	1



VZBUTALNA TABELA

Q ₁	Q ₂	Q ₁ (n+1)	Q ₂ (n+1)	D ₁	D ₂
0	0	0	1	0	1
0	1	1	0	1	0
1	0	0	0	0	0
1	1	X	X	X	X

$$D_1 = Q_2$$

$$D_2 = \overline{Q_1} \overline{Q_2} + Q_1 Q_2 = \text{XOR vrste}$$

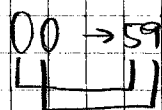
$$\Rightarrow \underline{Q_1 = Q_2}$$

$$X=0 : D_2 = \overline{Q_1} \cdot \overline{Q_2}$$

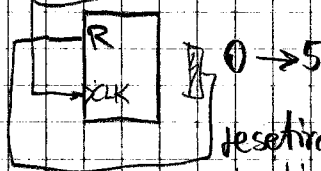
6. LAB. VATA c)

74LS390 → čip

2x DEKADNI ŠTEVEC ⇒ 0 → 9

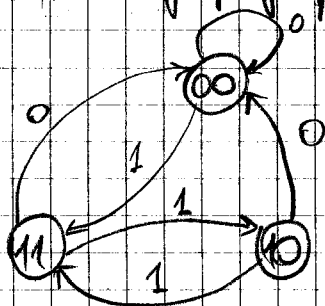


ASYNH



resetiramo, ko pride na 60 potem se takoj resetira.

3.) Iz podanega diagrama stanj zgradite sinhronsko sekvenco vezje. Uporabite T flip-flop

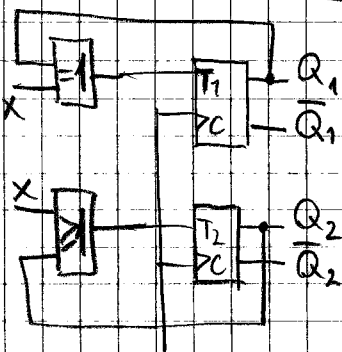


Q(n)	x=0	x=1
00	00	11
10	00	11
11	00	10
01	X	X

VZB. TABELA:

T zamenja stanje, če je 1, ohrani če je 0

X	Q ₁ (n)	Q ₂ (n)	Q ₁ (n+1)	Q ₂ (n+1)	T ₁	T ₂
0	0	0	0	0	0	0
0	0	1	0	1	0	0
0	1	0	1	0	1	1
0	1	1	1	1	0	0
1	0	0	0	0	0	0
1	0	1	0	1	0	0
1	1	0	1	0	1	1
1	1	1	1	1	0	0



$T_1: Q_2$

00	01	11	10
0	1	0	1
1	X	X	0

$T_2: Q_1$

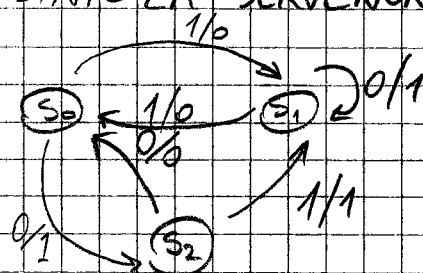
00	01	11	10
0	0	0	1
1	X	1	1

$$T_1: \bar{X}Q_1 + X\bar{Q}_1 = X \oplus Q_1 \leftarrow \text{XOR}$$

$$T_2: X - Q_2$$

22.12.2011

SINTEZA SEKVENCNIH VEZIJ



Iz podanega diagrama zgradite sekvenco vezje, J-K ff, ugotovite za katero vezje gre

1.) kodirna tabela:

$Q_1 Q_2$
S_0 00
S_1 01
S_2 10

2.) tabela stanj:

$Q(n)$	$Q(n+1)$ $X=0$	$X=1$
S_0	$S_2/1$	$S_2/0$
S_1	$S_1/1$	$S_0/0$
S_2	$S_0/0$	$S_1/1$

X	$Q_1(n)$	$Q_2(n)$	$Q_1(n+1)$	$Q_2(n+1)$	y	J_1	K_1	J_2	K_2
0	0	0	1	0	1	1	X	0	X
0	0	1	0	1	1	0	X	X	0
0	1	0	0	0	0	X	1	0	X
0	1	1	X	X	X	X	X	X	X
1	0	0	0	1	0	0	X	1	X
1	0	1	0	0	0	0	X	X	1
1	1	0	0	1	1	X	1	1	X
1	1	1	X	X	X	X	X	X	X

$Q(n)$	$Q(n+1)$	J	K
0	0	0	0
0	1	1	0
1	0	0	1
1	1	1	0

$y:$

00	01	11	10
0	0	0	0
1	0	X	0

$$y: \bar{X}\bar{Q}_1 + XQ_1 = X \equiv Q_1$$

$J_1: Q_1$

00	01	11	10
0	1	X	X
1	X	X	X

$K_1: Q_2$

00	01	11	10
0	X	1	1
1	X	X	X

$J_2: Q_1$

00	01	11	10
0	X	X	X
1	X	X	1

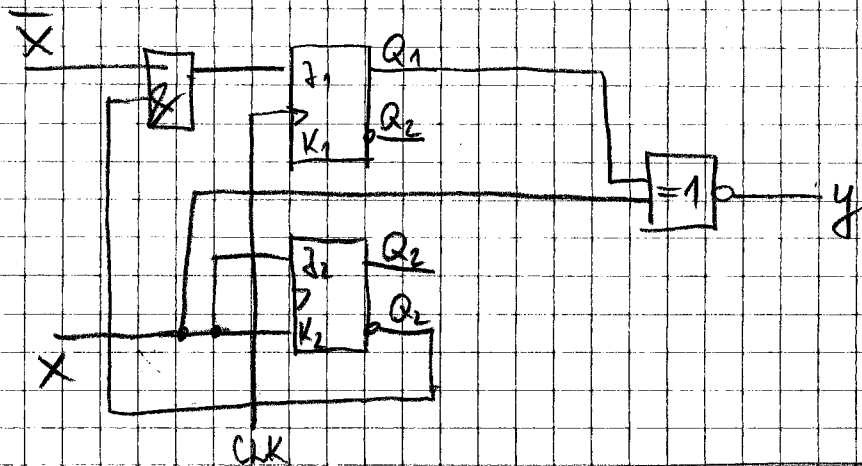
$K_2: X$

$$J_1: \bar{X}\bar{Q}_2$$

$$K_1: 1$$

$$J_2: Q_1$$

$$K_2: X$$



Prejšnje vezje spremenite v Moore-ovo

S_0
 S_1
 S_2

$y = 0$
 $y = 0, 1$
 $y = 1$

← S_1 razbijemo na dve stanji

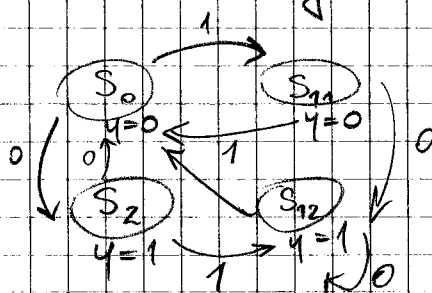
$S_{11}, y = 0$
 $S_{12}, y = 1$

1.) kodirane tabele

	Q_1	Q_2
S_0	0	0
S_{11}	0	1
S_{12}	1	0
S_2	1	1

	$Q(n+1)$		
$Q(n)$	$x=0$	$x=1$	y
S_0	S_2	S_{11}	0
S_{11}	S_{12}	S_0	0
S_{12}	S_{12}	S_0	1
S_2	S_0	S_{12}	1

2.) tabela stanj



$$J_1: \bar{X}$$

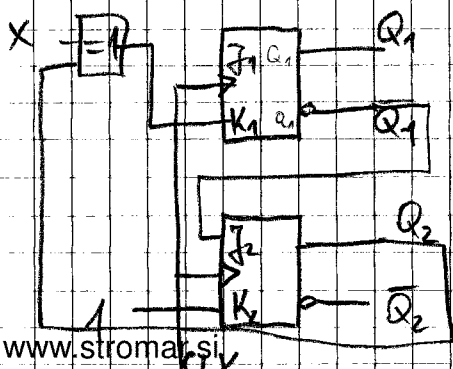
$$K_1: \bar{X}Q_2 + X\bar{Q}_2 = X \oplus Q_2$$

$$J_2: \bar{Q}_1$$

$$K_2: 1$$

$y: Q_1 \rightarrow$ Mooreov "avtomat"
ker izhod ni odvisen od vhoda

x	$Q(n)$	$Q_1(n)$	$Q_2(n)$	$Q_1(n+1)$	$Q_2(n+1)$	y	J_1	K_1	J_2	K_2
0	0	0	0	1	1	0	1	X	1	X
0	1	0	1	1	0	0	1	X	X	1
1	0	0	1	1	0	1	X	0	0	X
1	1	0	1	0	0	1	X	1	X	1
1	0	0	1	0	1	0	0	X	1	X
1	1	0	1	0	0	0	0	X	X	1
1	1	0	1	0	0	1	X	1	0	X



1.) Minimizirajte tabelo stanj:

sed. št.	x=0	x=1	y
S ₁	S ₃	S ₂	1
S ₂	S ₄	S ₃	1
S ₃	S ₅	S ₁	0
S ₄	S ₂	S ₅	1
S ₅	S ₃	S ₁	0

zdrúzujemo lahko le tista stanja, ki imajo enake izhode

A. B.	x=0	x=1	
S ₁ , S ₂	S ₃ , S ₄	S ₂ , S ₃	✓
S ₁ , S ₄	S ₃ , S ₂	S ₂ , S ₅	✓
S ₂ , S ₄	S ₄ , S ₂	S ₃ , S ₅	✓
S ₃ , S ₅	S ₃ , S ₃	S ₁ , S ₁	✓

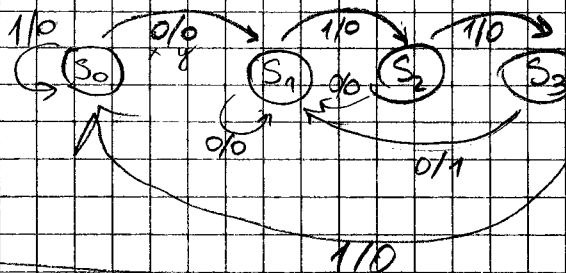
S₃=0
S₁=1
nista zdrúzljiva ⇒
tudi S₁, S₂ nista zdrúzljiva

S₁=S_A
S₂=S_B
S₃=S_C
n.s.
S₂ ≡ S₄
S₃ ≡ S₅

A. B.	x=0	x=1	y
S _A	S _C	S _B	1
S _B	S _B	S _C	1
S _C	S _C	S _A	0

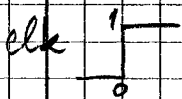
2.) Narišite diagram prehajanja stanj za sek. verzijo v Mealeyevi obliki, ki da na izhod 1, vsakeč ko se na izhodu pojavi sekvenca 0110

y: 1
x: 0110

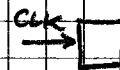


01100110
01101110

7. LAB. VAJA



Oznaka: PROCESS (CLK)
IF (CLK 'EVENT' AND CLK='1') THEN
STAVKI;
END IF;
END PROCESS



3.) Minimizacija

S. S.	x=0	x=1	y
S ₁	S ₂	S ₃	1
S ₂	S ₄	S ₆	1
S ₃	S ₆	S ₅	0
S ₄	S ₂	S ₇	1
S ₅	S ₆	S ₃	0
S ₆	S ₅	S ₄	0
S ₇	S ₆	S ₇	0

A. B.	x=0	x=1	
S ₁ , S ₂	S ₂ , S ₄	S ₃ , S ₅	✓
S ₁ , S ₄	S ₂ , S ₂	S ₃ , S ₇	✓
S ₂ , S ₄	S ₄ , S ₂	S ₆ , S ₇	✓
S ₃ , S ₅	S ₆ , S ₆	S ₅ , S ₃	✓
S ₃ , S ₆	S ₆ , S ₅	S ₇ , S ₄	✓
S ₄ , S ₇	S ₆ , S ₆	S ₅ , S ₇	✓
S ₅ , S ₆	S ₆ , S ₅	S ₄ , S ₄	✓
S ₆ , S ₇	S ₆ , S ₆	S ₃ , S ₇	✓
S ₇ , S ₇	S ₆ , S ₆	S ₄ , S ₇	✓

S₁, S₄ ≡ S_A
S₂ ≡ S_B
S₃, S₅ ≡ S_C
S₆ = S_D
S₇ ≡ S_C
S₃ = S₇ = S₅ = S_C

	$x=0$	$x=1$	y
s_A	s_B	s_C	$\frac{1}{2}$
s_B	s_A	s_B	$\frac{1}{2}$
s_C	s_B	s_C	0
s_D	s_C	s_A	0